

## **FISCAL POLICY AND INTEREST RATES IN A SMALL OPEN ECONOMY**

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*This paper contains an empirical investigation of the effects of fiscal policy on interest rates based on a conventional stochastic macro model designed for a small open economy. The empirical investigation utilizes data for Sweden, a country which has experienced very large fluctuations in the government budget deficits and in the short- and long-term nominal interest rates, thus providing a better empirical test than previous studies. According to the empirical results, larger budget deficits induce higher interest rates, as implied by conventional macroeconomic theory. (JEL: E12, E62, F41)*

### *1. Introduction*

In this paper I address the question of whether larger budget deficits produce higher interest rates. Theoretically it is well known that the effects of changes in fiscal policy on the term structure of interest rates are ambiguous. The Ricardian equivalence theorem states that, for a given path of government consumption expenditures, individuals view budget deficits as postponed tax-liabilities. Therefore budget deficits do not alter wealth, desired consumption paths or interest rates. According to the more

conventional view in macroeconomics, on the other hand, individuals do not fully internalize the future tax-liabilities, which implies that changes in government debt add to private wealth, influencing desired consumption paths and thus interest rates.<sup>1</sup> However, the empirical studies undertaken to date, mostly utilizing data for the United States, have not been able to supply either view with convincing evidence. Since the resolution of this issue is important for the design of macroeconomic policy, there is a need for more research in the field.

In this paper I utilize data for Sweden to provide a good empirical answer to the question posed above. The reason why Sweden is an interesting case is that the country has experienced very large fluctuations in the government budget deficits and short- and long term nominal interest rates since the beginning of the

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<sup>1</sup> When the term “conventional” is used, reference is made to Keynesian or other non-Ricardian models with rational expectations.

1980s. Consequently, this paper provides a high-powered empirical test compared to previous studies in the field.

Previous results in the literature have been obtained within three types of approach. The first is termed “conventional”, since it encompasses stochastic macro models, Keynesian or non-Ricardian, where agents are assumed to form their expectations rationally. Evans (1987a) develops a stochastic rational expectations model to study the proposition that larger budget deficits are associated with higher interest rates in a closed economy setting, and using data for a long sample period from the United States he provides evidence inconsistent with this proposition.<sup>2</sup> The same conclusion is reached using a data set containing six countries (Evans, 1987b).<sup>3</sup> Finally, Evans (1988) investigates whether forward rates in the United States during the second world war were an increasing function of government debt and find no evidence for such a positive relationship; rather, there is a negative relationship. Allen (1990) estimates a reduced form AS-AD model using quarterly data on various measures of the federal debt in the United States between 1961 and 1985, and finds that there is a positive and statistically significant linkage between government debt and a tax-adjusted short-term real interest rate. Allen (1992) models first differences in order to control for autocorrelation and intercept instability, and provides more empirical evidence of a positive and statistically significant relationship. There seems to be two potential explanations for the different results obtained by Allen and Evans. Allen chooses not to model a reduced form for the inflation expectations. Instead he uses proxies in the estimated equation. Moreover, Allen primarily considers alternative measures of debt, while Evans focuses on different measures of deficits.

The second type of model attempts to test the Ricardian equivalence theorem more directly.

The papers by Plosser (1982, 1987) are perhaps the most well known examples in a closed economy setting. In neither of his papers does Plosser find any statistically significant relation between deficits and interest rates in the United States. He interprets these findings as indirect evidence for the Ricardian view. Boothe and Reid (1989) extend the work of Plosser to the Canadian case, which they consider to be a small open economy. The empirical results of Boothe and Reid are also consistent with the previous studies undertaken by Evans and Plosser. In a political economy setting, Minford (1988) provides theoretical arguments against the Ricardian view. Minford then provides empirical evidence consistent with the predictions from the model, using annual data for the United Kingdom between 1920–1982.<sup>4</sup>

The third type of model considered in the literature is the so called “loanable funds” model. This type of model, which models interest rates as equilibrium responses to the demand and supply in the loan markets is used, for example, by Cebula et al. (1988), de Haan and Zelhorst (1990), Cebula et al. (1990), Cebula and Rhodd (1993), Correia-Nunes and Stemitiotis (1995) and Miller and Russek (1996).<sup>5</sup> The estimated equations in this literature are very similar; some nominal long-term interest rate is linearly related to a set of explanatory variables, including some measures of the expected inflation rate and government deficits and debts. Another characteristic of these studies is that they use annual data. The empirical evidence provided in this setting points in one direction: the level of nominal interest rates is positively related to government budget deficits.

The different findings in the literature raises the issue as to why the different results have

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<sup>2</sup> Evans (1985) investigates the empirical relationship between nominal and real interest rates and current and past government budget deficits in the United States, and finds no positive association.

<sup>3</sup> The six countries are: Canada, France, West Germany, Japan, United Kingdom and the United States.

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<sup>4</sup> It is notable that the parameterization in the model is not as parsimonious as in the other studies. He includes a measure of inflation expectations, dummies for the second world war and the Korean war etc. in his regression.

<sup>5</sup> Although not explicitly modeled, this literature generally acknowledge the effects of growing integration of world capital markets on the relationship between budget deficits and interest rates. Globalization of world financial markets in this context means that budget deficits may be financed by borrowing abroad, implying that the impact of deficits on national interest rates can be moderated.

been obtained. The literature cited above suggest two important factors. First of all, the data frequency seems to be important. In studies which have exploited lower frequency data, the evidence is more in favor of the conventional view and against the Ricardian view. Second, the treatment of the expected inflation rate seems to be of considerable importance. In the studies surveyed, the results tend to be more supportive of the conventional model when a proxy has been used to account for the expected inflation rate, rather than a reduced form. By including a proxy for expected inflation, one does not capture the indirect effects of budget deficits via expected inflation on interest rates.<sup>6</sup>

In this paper we will account for these two important factors as follows. First, by using both monthly and quarterly data in the estimations, we will be able to investigate the potential sensitivity of the results with respect to the data frequency. Second, by using the theoretical model to solve for the expected inflation rate as a function of macroeconomic variables (e.g. the budget deficit) and use these macro variables in the regression rather than a proxy for the expected inflation rate, we will be able to pin down the “true” effects of budget deficits on interest rates.

The empirical approach in this investigation is close to that of Evans (1985, 1987a, 1987b, 1988). First, I make a survey of the results in the previous literature and try to draw some important lessons for the investigation in this paper. Second, I set up a conventional stochastic macro model, in which the term structure of nominal interest rates is determined in terms of different policy variables, and use this model to study the effects of fiscal policy. Since Sweden is best characterized as a small open economy, a conventional stochastic macro model for a small open economy is constructed. The reason for spending time on this is that there has been little attention paid to the effects of fiscal poli-

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<sup>6</sup> *In most conventional macro models, a (temporary) increase in the budget deficit today, will raise the price level more today than expected future ones, leading to lower expected inflation rate today. As a result, the effects of budget deficits on interest rates will in general be upward biased when expected inflation enter as a separate variable in the regression.*

cy on the term structure in a small open economy.<sup>7</sup> In addition to providing a framework for the empirical research in this paper, this approach may also offer several important insights about this issue. For example, it is not obvious that larger budget deficits produce higher interest rates in a small open economy conventional model. Finally, I estimate the implied nominal interest rate regression equations on Swedish data, taking the lessons from the survey and the conventional model into account.

The empirical results suggest that larger budget deficits induce higher nominal interest rates. According to the empirical evidence, an increase in the budget deficit as a percentage of GDP by one percent leads to increases in the domestic short- and long term interest rates of approximately 0.20 percentage points after a period of two years.

The structure of the paper is as follows. In Section 2, the model is developed and solved for the nominal interest rates. The quarterly and monthly data set are discussed in Section 3. In Section 4, some empirical issues are discussed and the empirical results for Sweden are presented. Some tentative conclusions are then finally drawn in Section 5.

## *2. The yield curve in a conventional small open economy model*

In this section I construct and use a conventional stochastic macro model to illustrate the effects of fiscal policy on the term structure of nominal interest rates in a small open economy. The model is a straightforward small open economy extension of the model presented by

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<sup>7</sup> *In a closed economy setting Turnovsky (1989) develops and uses a stochastic macro model to study the effects of changes in macroeconomic policy on the term structure of real and nominal interest rates. A closely related paper is McCafferty (1986). Grinols and Turnovsky (1994) use stochastic calculus to study the interaction between exchange rates and interest rates in a small open economy, but without a term structure of interest rates explicitly incorporated. Finally, the seminal paper by Cox, Ingersoll and Ross (1985) contains the most general stochastic utility maximizing approach to the term structure of interest rates, but they do not explicitly consider changes in macroeconomic policy.*

Turnovsky (1989). For ease of exposition, no dynamics are explicitly considered, but of course, in an empirical analysis of real world data, dynamics are important. Therefore, one can view the parameters in the theoretical model below as stationary polynomials in the lag operator.

### 2.1 The model

The aggregate supply function is given by

$$(1) \quad y_t = \beta(p_t - E_{t-1}p_t) + \varepsilon_t^{AS},$$

where  $y_t$  denotes real output gap in natural logs in time period  $t$ ,  $p_t$  the price of  $y$  in natural logs and  $E_{t-1}p_t$  the expectation of the price level in  $t$  conditional on all available information in  $t-1$ . In (1),  $\varepsilon_t^{AS}$  is interpreted as an exogenous white noise productivity shock.

Aggregate demand in the model is described by the IS-LM equations. The IS curve is given by

$$(2) \quad y_t = -\lambda_1 r_t^l + \lambda_2 g_t + \lambda_3 D_t + \lambda_4 (s_t + p_t^* - p_t) + \varepsilon_t^{IS} \\ \equiv -\lambda_1 r_t^l + X_t + \lambda_4 (s_t - p_t) + \varepsilon_t^{IS}$$

where  $r_t^l$  denotes the domestic long-term real interest rate in natural units,  $g$  real government spending in natural logs,  $D$  real government budget deficit,  $s$  the nominal exchange rate in natural logs,  $p^*$  the foreign price level in natural logs and  $X \equiv \lambda_2 g + \lambda_3 D + \lambda_4 p^*$  is just a convenient notation. As in Turnovsky (1989), the relevant interest rate in (2) is taken to be the domestic long-term real interest rate. The IS curve implicitly captures the conventional mechanism that government budget deficits add to private wealth, influencing desired consumption paths and thus output and interest rates for a given exchange rate and a given domestic price level. Money market equilibrium is described by the LM curve

$$(3) \quad m_t - p_t = \alpha y_t - \gamma i_t^s + \varepsilon_t^{LM},$$

where  $m$  denotes the nominal money supply in natural logs and  $i^s$  the domestic nominal short-term interest rate. Thus, as in Turnovsky (1989), the demand for money is assumed to depend on

the short-term nominal interest rate. In (2) and (3),  $\varepsilon_t^{AS}$  and  $\varepsilon_t^{LM}$  are interpreted as real demand and money demand shocks, respectively. It is assumed that the parameters in (1), (2) and (3), denoted  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\lambda_1$ ,  $\lambda_2$ ,  $\lambda_3$  and  $\lambda_4$ , are all positive, which is standard in conventional macro models.

The financial part of the model involves the relationships between the domestic and foreign short- and long-term real and nominal interest rates.<sup>8</sup>

The Fisher equations which relate domestic nominal and real interest rates are

$$(4) \quad i_t^s = r_t^s + (E_t p_{t+1} - p_t)$$

and

$$(5) \quad i_t^l = r_t^l + \frac{1}{2} (E_t p_{t+2} - p_t)$$

where  $r^s$  = domestic short-term real interest rate and  $i^l$  = domestic long-term nominal interest rate.

The equations which describe the real and nominal term structures of interest rates are given by

$$(6) \quad i_t^l = \frac{1}{2} (r_t^s + E_t r_{t+1}^s)$$

and

$$(7) \quad i_t^l = \frac{1}{2} (i_t^s + E_t i_{t+1}^s).$$

The uncovered interest parity, UIP, condition, which relates the domestic short- and long-term nominal interest rates to their foreign counterparts, denoted  $i^{s*}$  and  $i^{l*}$ , and the expected one and two period changes in the nominal exchange rate are

$$(8) \quad i_t^s - i_t^{s*} = \Delta E_t s_{t+1}$$

and

<sup>8</sup> In accordance with Turnovsky (1989), it is assumed that there exist two types of domestic and foreign (zero coupon) assets with one and two periods to maturity. It is then straightforward to derive equations (6), (7), (8) and (9) up to a constant risk-premium as simple asset pricing relationships.

$$(9) \quad i_t^l - i_t^{l*} = \frac{1}{2} (E_t s_{t+2} - s_t).$$

In order to close the model, we need to make some additional assumptions. First, in conventional macro models,  $g$  and  $D$  are normally considered to be exogenous. We will adopt this approach throughout the theoretical analysis in this paper. Second,  $p^*$ ,  $i^{s*}$  and  $i^{l*}$  will also be treated as exogenous to the domestic economy, which is quite natural in a small open economy framework. Finally, we need to specify a policy rule for  $m$ . In theoretical analysis, it is standard to assume that  $m$  is independent of the other exogenous variables. Since the main interest in this paper is the interaction between fiscal policy and the term structure, we adopt this assumption in the theoretical part of the paper. However, in an analysis of real world data, this strategy may lead to problems, since, for instance, the monetary policy rule is unlikely to be independent of  $g$  and  $D$ . Therefore, the first and third assumptions are relaxed in the empirical analysis in this paper.

## 2.2 Determination of nominal interest rates

To derive analytical solutions for the endogenous variables  $i^s$  and  $i^l$  in terms of current and expected future values of the exogenous variables  $g$ ,  $D$ ,  $m$ ,  $p^*$ ,  $i^{s*}$  and  $i^{l*}$ , we proceed by first determining price level expectations, and then substitute the resulting expressions back into the system to solve for  $s_t$ . Finally, the solution for  $s_t$  is used in the UIP conditions to derive the solutions for the short- and long-term domestic nominal interest rate differentials  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$ .<sup>9</sup>

By this procedure the short- and long-term interest rate differentials depend both on the period  $t$  and  $t-1$  expected discounted sums of nominal money supplies, government expenditures and deficits, foreign price level and short-term nominal interest rates and the period  $t$  expected discounted sum of foreign long-term nominal interest rates. More formally, let  $\psi_j^{i^s, D}$

and  $\psi_j^{i^l, D}$  measure the impact of period  $t$  expected budget deficits,  $E_t D_{t+j}$ ,  $j=0, 1, 2, \dots$  periods ahead on the short- and long-term interest rate differentials, respectively (analogous notation for the other variables  $g$ ,  $p^*$ ,  $m$ ,  $i^{s*}$  and  $i^{l*}$  as well). Since the  $\psi_j^{i^s}$  and  $\psi_j^{i^l}$  coefficients are quite messy to evaluate analytically for  $j > 1$ , I have made simulations conditional on some not a priori unreasonable values for  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\lambda_1$  and  $\lambda_4$  in order to get a feeling for the size and magnitude of the paths for them.<sup>10</sup> For simplicity, it is assumed that  $\lambda_2 = \lambda_3 = 1$ , so that  $\psi_j^{i^s, g} = \psi_j^{i^s, D}$  and  $\psi_j^{i^l, g} = \psi_j^{i^l, D}$  hold for all  $j$ . The resulting paths for  $j=0, 1, 2, \dots, 40$  are depicted in Figures 1 and 2 for  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$ , respectively. In Figures 1 and 2, the dashed lines refer to the  $\psi_j^{i^s}$  and  $\psi_j^{i^l}$  coefficients, while the solid lines refer to the accumulated effects in period  $t+j$ , measured as  $\sum_{n=0}^j \psi_n^{i^s}$  and  $\sum_{n=0}^j \psi_n^{i^l}$ .

As seen from Figure 1, all the  $\psi_j^{i^s}$  coefficients range from positive to negative values for  $j=0, \dots, 40$ ; for  $j=0$ ,  $\psi_0^{i^s, g}$ ,  $\psi_0^{i^s, D}$  and  $\psi_0^{i^s, p^*}$  are positive while  $\psi_0^{i^s, m}$ ,  $\psi_0^{i^s, s}$  and  $\psi_0^{i^s, i^*}$  are negative, which can be demonstrated analytically. The coefficients for the foreign price level are very similar to those of government expenditures and budget deficit since the chosen value of  $\lambda_4$  is close to 1. Turning to Figure 2, we find that the same conclusion apply after the second period, e.g. it can be shown that  $\psi_0^{i^l, D}$  and  $\psi_1^{i^l, D}$  are always positive. It is interesting to note that the simulated paths for the budget deficit in Figures 1 and 2 compare well qualitatively with the closed economy results in Turnovsky (1989), in the sense that the  $\psi_{t+j}^{i^s, D}$  and  $\psi_{t+j}^{i^l, D}$  coefficients are both positive and negative, but poorly with Evans (1987a), where all the corresponding  $\psi_j^{i^s, D}$  and  $\psi_j^{i^l, D}$  coefficients are found to be greater than zero. It can be shown that this result is due to the introduction of a term structure within the model; see Turnovsky (1989) for a deeper discussion about the intuition.

From Figures 1 and 2 we also see that the accumulated effects of an period  $t$  permanent

<sup>9</sup> All the derivations of the equations informally presented and analyzed in this section are provided in Appendix A.

<sup>10</sup> The values for  $\alpha$  and  $\gamma$  are taken from Goldfeld and Sichel (1990) and set to 0.6179 and 0.2170 respectively.  $\lambda_1$  and  $\beta$  are taken from Söderlind (1997) and set to 5 and 500 respectively.  $\lambda_4$  is taken from Hansson (1993) and set to 0.9644.

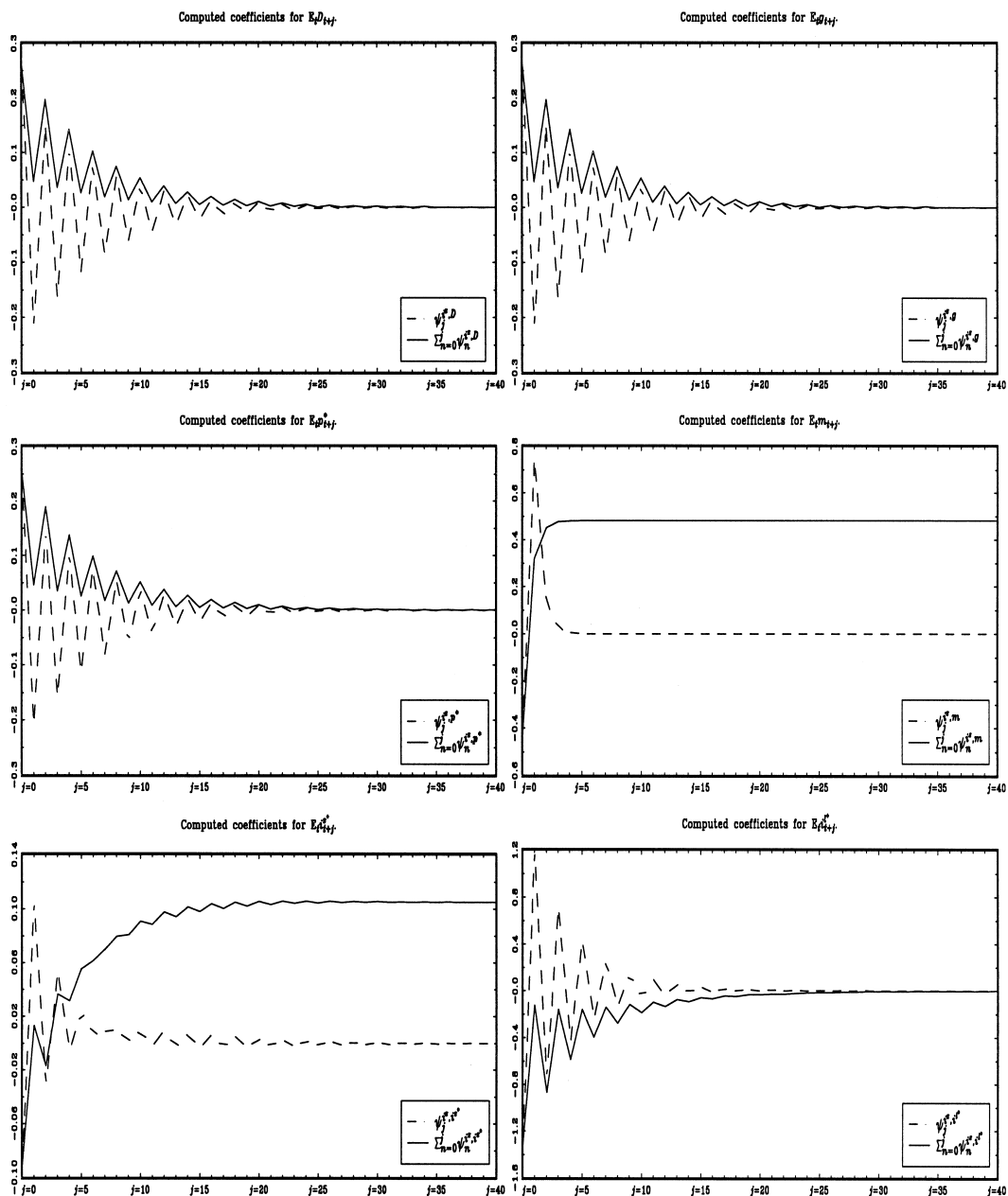


Figure 1. Effects on  $i_t^* - i_t^{**}$  of exogenous variables  $j$  periods ahead.

expected change in  $g$ ,  $D$ ,  $p^*$  and  $i^{l*}$  go towards zero when  $j$  increases. This result is due to the small open economy assumption; for example, after an period  $t$  permanent expected change (unknown in period  $t-1$ ) in the budget deficit, the nominal exchange rate today,  $s_t$ , and the pe-

riod  $t$  expected exchange rates in period  $t+1$  and  $t+2$ ,  $E_t s_{t+1}$  and  $E_t s_{t+2}$ , change by the same amount. Via the UIP conditions (8) and (9), the effects on the short- and long-term interest rate differentials are then zero. This result is important since it suggests that the effects of budget

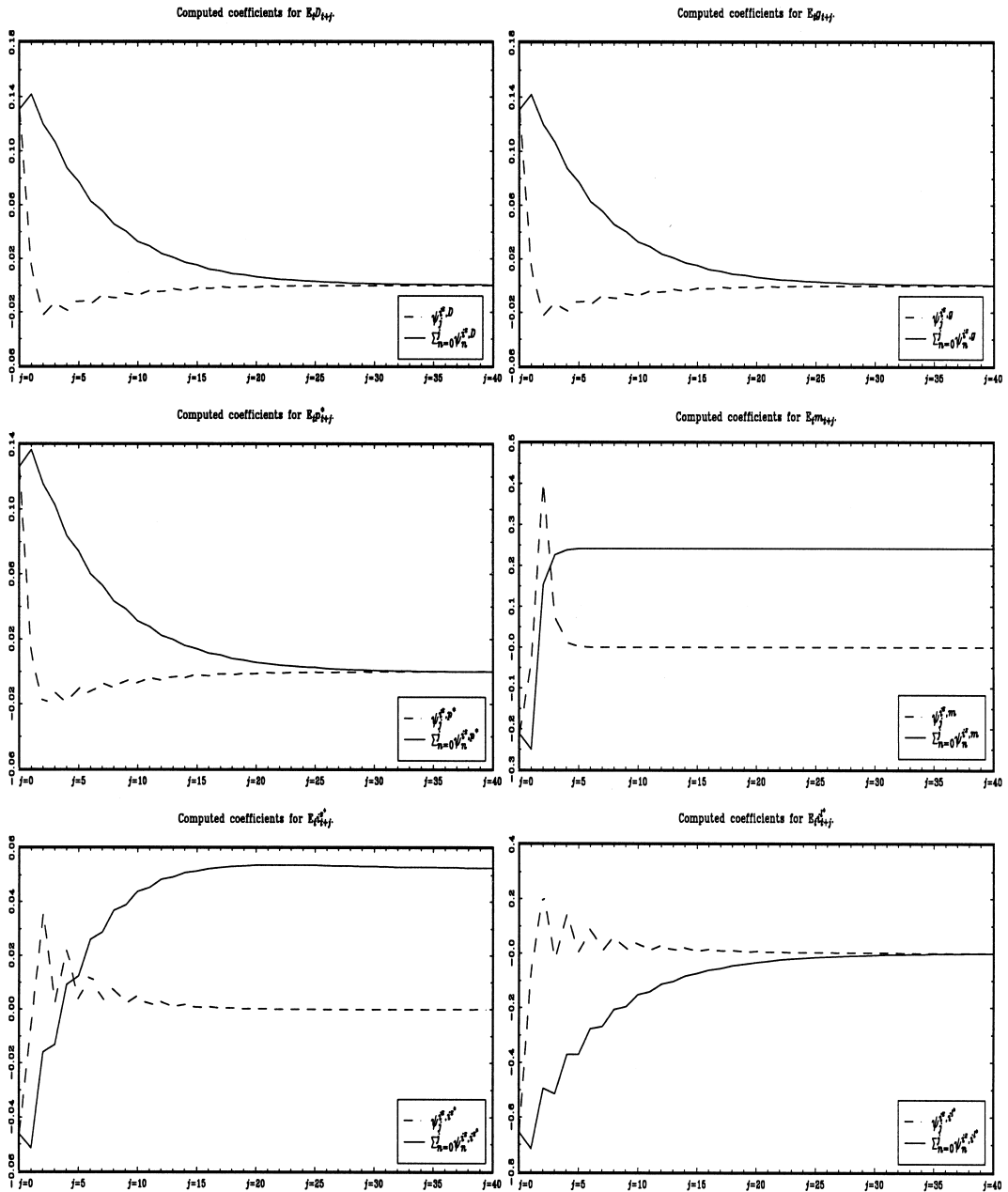


Figure 2. Effects on  $i_t^e - i_t^{e*}$  of exogenous variables  $j$  periods ahead.

deficits on interest rates in a small open economy framework are likely to be small if the budget deficit can be characterized as (or close to) a random walk.

Finally, the long-run accumulated effects of an period  $t$  (unknown in period  $t-1$ ) expected

increase in money supply and the foreign short-term nominal interest rate are positive and exactly half as large on the long-term interest rate differential compared to the short-term interest differential. The intuition behind this result is that the period  $t-1$  expected price level in pe-

riod  $t$ ,  $E_{t-1}p_t$ , is unaffected, so that also  $s_t$  is unaffected in this respect by permanent expected increases in  $m_t$  and  $i_t^{s*}$ . But expected permanent increases in  $m_t$  and  $i_t^{s*}$  increase the period  $t$  expected future price level in the periods  $t+1$  and  $t+2$ ,  $E_t p_{t+1}$  and  $E_t p_{t+2}$ , in this respect and thereby also  $E_t s_{t+1}$  and  $E_t s_{t+2}$  with the same amount. Via the UIP conditions (8) and (9), we then get an increase in  $i_t^l - i_t^{l*}$  that is exactly half as large as the increase in  $i_t^r - i_t^{r*}$ <sup>11</sup>

### 2.3 Empirical implementation of the model

In order to generate empirically testable implications for the nominal short- and long-term interest rate differentials, we need to make some assumptions regarding the stochastic processes for the exogenous variables, and thus how the expectations for these variables are formed.

Here it is assumed that the exogenous vector of variables  $z_t^T \equiv [p^* \ i_t^{s*} \ i_t^{l*} \ g \ D \ m]$  evolves according to a VAR( $p$ ) process

$$(10) \quad z_{t+1} = \rho^z(L) z_t + \varepsilon_{t+1}^z,$$

where  $\rho^z(L) \equiv \sum_{i=0}^p \rho_i^z L^i$  and the errors in  $\varepsilon^z$  are normally distributed and serially uncorrelated with  $E_t \varepsilon_{t+j}^z = 0$  for all  $j > 0$  with a positive definite covariance matrix. This is a conventional assumption in empirical analysis, and for instance Evans (1987a) uses an assumption similar to (10). The specification in (10) relaxes the earlier assumption of independently distributed exogenous variables. For example, it allows for money supply to be determined by some policy function of the other exogenous variables.<sup>12</sup>

Using (10) it can be shown that the solutions for the interest rate differentials are of the following general form

$$(11) \quad i_t^r - i_t^{r*} = \delta_0^r + \delta^r(L) z_t + v_t^r$$

<sup>11</sup> However, this result is sensitive to the parameterization of the model. With the numerical assumptions about  $\alpha$ ,  $\lambda_1$  and  $\lambda_4$  here, it is the case that  $\alpha(\lambda_1 + 2\lambda_4) - 2 > 0$ . But if  $\alpha(\lambda_1 + 2\lambda_4) - 2 < 0$ , permanent increases in  $m_t$  and  $i_t^{s*}$  have negative accumulated effects on  $i_t^l - i_t^{l*}$  and  $i_t^r - i_t^{r*}$ .

<sup>12</sup> Note also that from now on, dynamics are explicitly considered in the model. That is, we use the implicit assumption that all the parameters are stationary lag polynomials, i.e.  $\alpha \equiv \alpha(L)$ ,  $\beta \equiv \beta(L)$  and so forth.

where  $\delta^r(L) \equiv [\delta^{r,s}(L), \delta^{r,D}(L), \delta^{r,p^*}(L), \delta^{r,m}(L), \delta^{r,i^{s*}}(L), \delta^{r,i^{l*}}(L)]$  for  $r = s, l$ .<sup>13</sup> However, in this general case, nothing can be said about the sums of the individual parameters in the lag polynomials in  $\delta^r$ ; the sign and size of these sums will ultimately depend on the coefficients in  $\rho^z(L)$ . In this sense, it is fair to say that it is essentially an empirical question whether larger government budget deficits lead to higher interest rates; that is, whether the sums of the coefficients in the lag polynomials  $\delta^{s,D}(L)$  and  $\delta^{l,D}(L)$ , equal to  $\sum \delta_i^{s,D} L^i$  and  $\sum \delta_i^{l,D} L^i$  respectively, are positive or negative.

However, if we make the simplifying assumption that  $\rho^z(L) \equiv \rho^z$ , where  $\rho^z$  is a diagonal matrix with the elements  $[\rho^{p^*} \ \rho^{p^*} \ \rho^{i^{s*}} \ \rho^{i^{s*}} \ \rho^g \ \rho^D]$  in the diagonal, it is possible to draw further conclusions. In this case, the solution for the interest rate differentials is

$$(12) \quad \begin{aligned} i_t^r - i_t^{r*} = & \delta_0^r + \delta_1^r(L) g_t + \delta_2^r(L) D_t + \delta_3^r(L) p_t^* \\ & - \delta_4^r(L) m_t - \delta_5^r(L) i_t^{s*} - \delta_6^r(L) i_t^{l*} \\ & + \delta_7^r(L) \Delta g_t + \delta_8^r(L) \Delta D_t + \delta_9^r(L) \Delta p_t^* \\ & + \delta_{10}^r(L) \Delta m_t + \delta_{11}^r(L) \Delta i_t^{s*} + v_t^r. \end{aligned}$$

for  $r = s, l$ . By introducing the notation

$$\begin{aligned} \delta^r(L) \equiv & \begin{bmatrix} \delta_1^r(L) + \delta_7^r(L)(1-L), & \delta_2^r(L) + \delta_8^r(L) \\ (1-L), & \delta_3^r(L) + \delta_9^r(L)(1-L), -\delta_4^r(L) \\ + \delta_{10}^r(L)(1-L), & -\delta_5^r(L) + \delta_{11}^r(L)(1-L), \\ -\delta_6^r(L) \end{bmatrix} \\ \equiv & \begin{bmatrix} \delta^{r,s}(L), \delta^{r,D}(L), \delta^{r,p^*}(L), \delta^{r,m}(L), \\ \delta^{r,i^{s*}}(L), \delta^{r,i^{l*}}(L) \end{bmatrix} \end{aligned}$$

the solution can be written in the general form considered in (11). With this additional assumption, the model has some nice implications. It is now the case that all the parameters in the lag polynomials  $\delta_i^r(L)$  for  $i = 1, \dots, 6$  are positive provided that  $\{\rho^g, \rho^D, \rho^{p^*}, \rho^m, \rho^{i^{s*}}, \rho^{i^{l*}}\} \in (0, 1)$ . This implies that the sums of the polynomials  $\delta^{r,s}(L)$ ,  $\delta^{r,D}(L)$  and  $\delta^{r,p^*}(L)$ , are always positive while  $\delta^{r,m}(L)$ ,  $\delta^{r,i^{s*}}(L)$  and  $\delta^{r,i^{l*}}(L)$  are negative. However, with the exception of  $\delta^{r,i^{l*}}(L)$ , the same conclusion cannot be made for all the in-

<sup>13</sup> All the derivations of the equations presented in this section are provided in Appendix A.



dividual parameters in these polynomials; the sign of them can alternate over time. The reason is that changes in the exogenous variables have effects on the interest rate differentials via the lag polynomials  $\delta_i^r(L)$  for  $i=7, \dots, 11$ , and that the signs of the parameters in these lag polynomials are ambiguous. Indeed, these theoretical predictions are different from those of Allen (1990, 1992) and Evans (1985, 1987a, 1987b), since their models did not imply these ambiguities for the individual parameters. The reason why this difference occur is that I have an aggregate supply function in the model, which makes it possible to explicitly solve for the price level expectations. The fact that I use a small open economy model with a term structure of interest rates does not matter for this result.

In addition, if  $\rho^z = I_6$ , then the variables  $g$ ,  $D$ ,  $p^*$  and  $i^{l*}$  do not have any effects neither on the short- nor the long-term interest rate differentials. In this case, only changes in money supply and the foreign nominal short-term interest rate influence  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$  via changes in the expected price level. The intuition behind this result is straightforward. Consider, for example, an increase in the budget deficit in period  $t$ . If  $\rho^D$  is equal to one, then the nominal exchange rate today,  $s_t$ , and the expected exchange rate in the periods  $t+1$  and  $t+2$ ,  $E_t s_{t+1}$  and  $E_t s_{t+2}$ , will be fully adjusted downwards by the same amount ( $s_t$  appreciates), thus leaving  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$  unaffected via the UIP conditions. But if  $\rho^D$  is less than one, then the nominal exchange rate  $s_t$  is still fully adjusted, while  $E_t s_{t+1}$  and  $E_t s_{t+2}$  are only partially adjusted downwards, thus increasing  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$  via the UIP conditions since  $\Delta E_t s_{t+1}$  and  $E_t s_{t+2} - s_t$  become positive. Moreover, since it is plausible to assume that all the parameters  $\rho^g$ ,  $\rho^{p^*}$ ,  $\rho^m$ ,  $\rho^{is^*}$  and  $\rho^{il^*}$  are equal or very close to one, we do not expect any of these variables to have any large level effects on the short- and long-term interest rate differentials. It also seems reasonable to assume that  $\rho^D$  is high, but slightly less than one, which implies that an increase in the budget deficit will increase  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$  by a relatively small amount. Thus, if  $\rho^D$  is sufficiently close to one, the effect of changes in the budget deficit on  $i_t^s - i_t^{s*}$  and  $i_t^l - i_t^{l*}$  will be almost

zero, independently of the monetary policy rule. However, it should be emphasized that these last results are due to the small open economy feature of the model.

The interesting implication of these results is that a simple conventional macroeconomic model may offer a possible explanation for the lack of empirical relationship between government budget deficits and interest rates. That is, when empirical analyses based on (11) are carried out, one might easily obtain “wrong” results because it may very well be the case that the true sum of the elements in the lag polynomials for  $D_t$  is very close to zero, which makes it hard to pin down the correct relationship empirically. In particular this is true if data with low sample variability is used.

(11) provides the framework for the empirical investigation that follows below, and it should therefore be noted that the exogenous shocks  $v_t^r$  are very likely to be serially correlated over time.<sup>14</sup>

### 3. Data

Since the Swedish financial markets were heavily regulated until the beginning of the 1980s, it is hard to acquire good interest rate data for long samples for Sweden. In this paper, interest rates on a three-month government Treasury bill and a five- to ten-year government Treasury bond are used as measures of  $i^s$  and  $i^l$  (expressed as effective yields). Data of good quality on these two series are available from January 1982 and the middle of February 1984 respectively.<sup>15</sup> Monthly frequency until June 1996 then gives 174 observations, while quarterly frequency gives at the most only 58. Since the survey of earlier empirical literature suggested that a different choice of data frequency

<sup>14</sup> Since I consider the parameters to be stationary lag polynomials, i.e.  $\alpha \equiv \alpha(L)$ ,  $\beta \equiv \beta(L)$  and so forth, the model implies that the error terms in (11),  $v_t^s$  and  $v_t^l$ , are moving average (MA) terms.

<sup>15</sup> To get an indication of the robustness with respect to the choice of maturity for the short-term Treasury bill for the empirical investigation, other Treasury bills with one, six and twelve months to maturity have been examined, and the results were found to very similar.

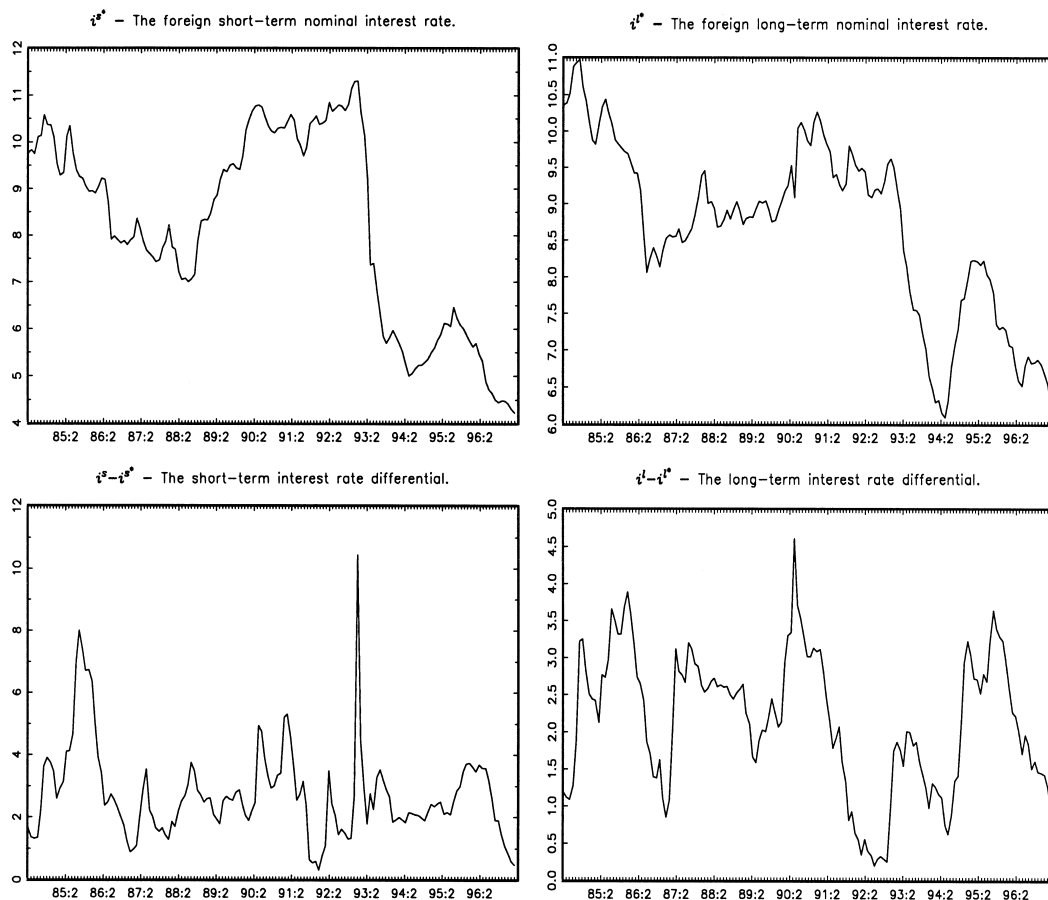


Figure 3. Monthly data on nominal interest rates.

has been important for different empirical evidence, we will use both monthly and quarterly to take this aspect into account. Unfortunately the highest frequencies for  $g$  and  $y$  are quarterly.<sup>16</sup> Hence, in order to be able to use monthly data in the regressions, some kind of interpolation for these two variables was necessary. I therefore assumed that, first,  $g$  is uniformly distributed over the months within each quarter and, second, that the monthly distribution of  $y$  within the quarters follows the private industrial production, denoted  $x$ , according to the scheme  $y_{month,t} = \kappa_q(t)x_{month,t}$  where  $\kappa_q(t) \equiv \frac{y_{q,q(t)}}{x_{q,q(t)}}$  and

$q(t) = 1$  for all  $t = 1, 2, 3$ ,  $q(t) = 2$  for all  $t = 4, 5, 6$  etc. The principal reason for the need to use  $y$  is the presumption that the Swedish economy has the property of homogeneity; that is, doubling government consumption and deficits and nominal money supply and the size of the economy leaves the interest rate differentials unaffected. A very natural way to accomplish this is to divide  $g$ ,  $D$  and  $m$  with  $y$ . Evans (1987a) uses the same approach.

Since Sweden had a fixed exchange rate regime between 1982 and November 1992, and thus for the greater part of the sample period, “currency-basket” weighted foreign short- and longterm interest rates (effective yields) and price levels have been constructed to obtain measures of  $i^{s*}$ ,  $i^{l*}$  and  $p^*$ . When there has been

<sup>16</sup> From now on,  $y$  denotes the gross domestic product, GDP, and not the log of the output gap.

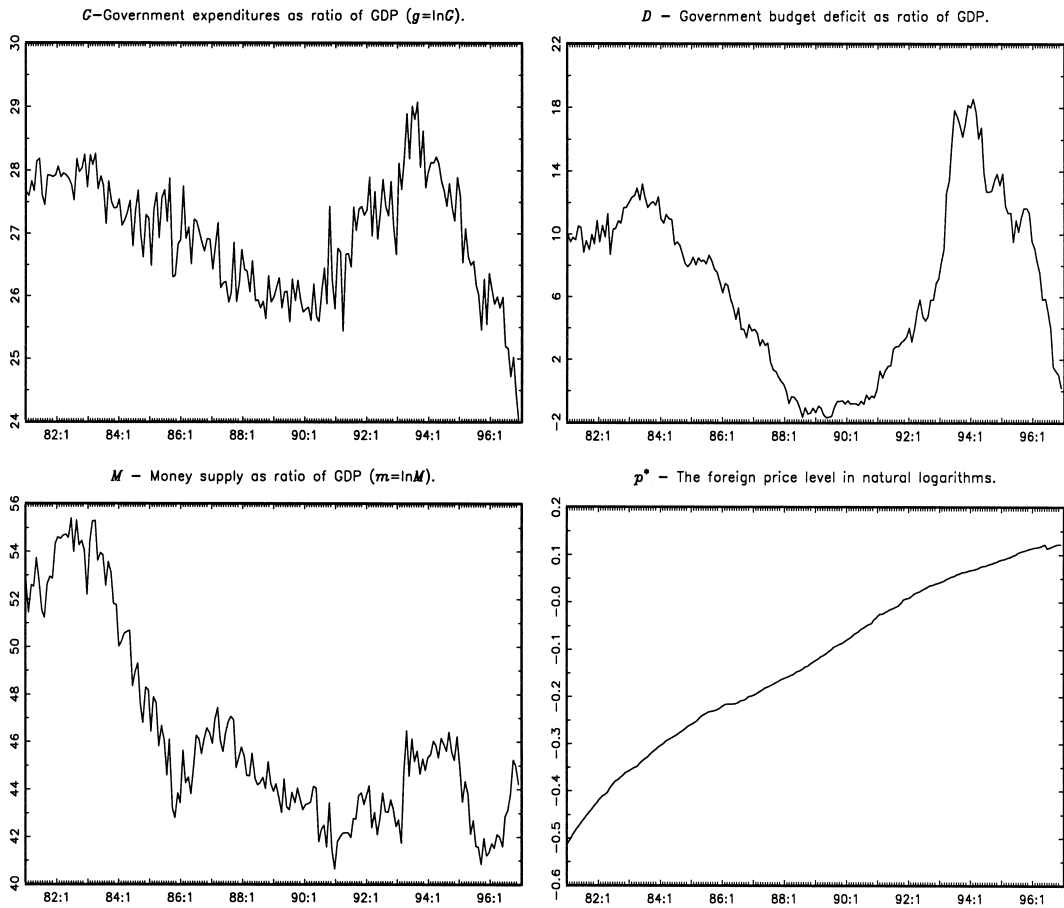


Figure 4. Monthly data on seasonally adjusted macrovariables.

no possibility of acquiring interest rate data for certain countries during limited periods in the sample, the “currency-basket” weights have been normalized to one.<sup>17</sup> The calculated series for  $i^{s*}$ ,  $i^{l*}$ ,  $i^s - i^{s*}$  and  $i^l - i^{l*}$ , and  $g$ ,  $D$ ,  $m$  and  $p^*$  are depicted in Figures 3 and 4 respectively.<sup>18</sup>

<sup>17</sup> This has not been a significant problem though; countries which together make up at least 67.10 percent in the beginning and up to 100 percent at the end of the sample period are included in the calculation of the foreign long-term interest rate. The corresponding figures for the short-term interest rate are 100 percent until November 1992, and thereafter between 79.9 to 97.54 percent.

<sup>18</sup> Note that the macroeconomic variables  $g$ ,  $D$ ,  $m$  and  $p^*$  have been subjected to seasonal adjustment. Since there seemed to be tendencies of changing seasonal pattern in most of the data series, the X11-method was used to deseasonalize the data. However, since the large and changing

Summary statistics for quarterly and monthly data are given in Tables 1 and 2 respectively.<sup>19</sup> In general, Tables 1 and 2 show that the sample autocorrelations are very high and taper off slowly over time, with the possible exception of  $i^s - i^{s*}$  and  $i^l - i^{l*}$ . This pattern is normally an indication that the variables may be non-stationary. The tables also show that the premium has on average been higher on  $i^s - i^{s*}$  compared to  $i^l - i^{l*}$ . The variance is also higher for

monthly seasonal variation in the private industrial production ( $x_m$ ), used to generate a measure of monthly GDP ( $y_m$ ), could not be sufficiently well deseasonalized with the X11-method, I used deseasonalized raw data on  $y_q$  and  $x_m$  to calculate  $y_m$ .

<sup>19</sup> Exact definitions and sources of all the variables used are given in Appendix B.

Table 1. Summary statistics for quarterly data.

Variable	Mean	Std.dev.	Sample autocorrelations					
			$\hat{\rho}_1$	$\hat{\rho}_2$	$\hat{\rho}_3$	$\hat{\rho}_4$	$\hat{\rho}_8$	$\hat{\rho}_{12}$
$i^s$	10.92	2.68	0.82	0.64	0.50	0.33	0.12	-0.12
$i^{s*}$	8.60	2.36	0.89	0.73	0.61	0.49	0.22	-0.06
$i^s - i^{s*}$	2.65	1.29	0.56	0.23	0.03	-0.23	-0.15	0.03
$i^l$	10.80	1.71	0.84	0.62	0.39	0.21	0.20	0.14
$i^{l*}$	9.13	1.69	0.94	0.85	0.76	0.65	0.40	0.28
$i^l - i^{l*}$	2.13	0.91	0.75	0.43	0.18	-0.07	0.03	-0.09
$g$	3.26	0.05	0.94	0.89	0.85	0.80	0.58	0.37
$D$	5.53	4.55	0.95	0.88	0.81	0.71	0.35	-0.05
$m$	3.85	0.12	0.97	0.94	0.91	0.88	0.75	0.65
$p^*$	-0.15	0.20	0.95	0.90	0.85	0.80	0.61	0.45

Note:  $g$ ,  $D$ ,  $m$  and  $p^*$  have been subjected to seasonal adjustment.  $g$ ,  $m$  and  $p^*$  are in natural logs.

Table 2. Summary statistics for monthly data.

Variable	Mean	Std.dev.	Sample autocorrelations						
			$\hat{\rho}_1$	$\hat{\rho}_6$	$\hat{\rho}_{12}$	$\hat{\rho}_{18}$	$\hat{\rho}_{24}$	$\hat{\rho}_{30}$	$\hat{\rho}_{36}$
$i^s$	10.92	2.76	0.91	0.59	0.30	0.18	0.12	0.04	-0.11
$i^{s*}$	8.60	2.36	0.97	0.73	0.48	0.32	0.22	0.11	-0.06
$i^s - i^{s*}$	2.65	1.46	0.76	0.16	-0.20	-0.24	-0.10	0.05	0.02
$i^l$	10.81	1.71	0.96	0.59	0.18	0.08	0.20	0.30	0.11
$i^{l*}$	9.35	1.67	0.98	0.84	0.64	0.48	0.40	0.31	0.18
$i^l - i^{l*}$	2.15	0.93	0.92	0.41	-0.08	-0.15	-0.01	0.14	-0.10
$g$	3.27	0.06	0.80	0.77	0.71	0.59	0.47	0.42	0.32
$D$	5.63	4.74	0.98	0.89	0.72	0.56	0.37	0.17	-0.02
$m$	3.91	0.12	0.95	0.91	0.85	0.78	0.74	0.71	0.67
$p^*$	-0.15	0.20	0.98	0.90	0.80	0.70	0.61	0.53	0.45

Note:  $g$ ,  $D$ ,  $m$  and  $p^*$  have been subjected to seasonal adjustment.  $g$ ,  $m$  and  $p^*$  are in natural logs.

the bills, both Swedish and foreign, than the bonds. Among the macroeconomic variables, the variance in  $D$  is much higher than the variability in  $g$  and  $m$ . This is a remarkable fact, since Plosser (1987) reports variabilities in  $g$  and  $m$  which exceed the variability in  $D$  by far for the United States. For instance, Plosser (1987) reports that the ratios between the standard deviation in  $g$  to  $D$  and in  $m$  to  $D$  are 7.3 and 2.1 on the monthly frequency. In this data set, the corresponding figures are 0.35 and 0.81. Of course, the high volatility in  $D$  reflects the dramatic swings in the Swedish budget deficits, which can be seen in Figure 4.

To summarize, the data set utilized in this paper provide a better possibility to identify the

the correct relationship between budget deficits and interest rates than in previous studies.

#### 4. Estimation and empirical results

This section deals with the problem of how to estimate (11) in an appropriate way and then reports the results of the regressions.

##### 4.1 Non-stationarity

As already noted in Section 3, one striking feature of the sample autocorrelations is that they start at very high values and then taper off very gradually. This pattern is generally an in-

Table 3. Augmented Dickey-Fuller tests of integration order on levels.

Variable	Quarterly frequency					Monthly frequency				
	const/ trend	$T$	$p$	$\hat{\phi}$	$t$ -value	const/ trend	$T$	$p$	$\hat{\phi}$	$t$ -value
$i^s$	yes/yes	51	4	-0.105	-1.465	yes/yes	158	9	-0.060	-1.581
$i^{s*}$	yes/yes	56	3	-0.056	-1.116	yes/yes	166	13	-0.012	-1.063
$i^s - i^{s*}$	yes/no	48	7	-0.794	-3.218**	yes/no	157	10	-0.306	-3.588***
$i^l$	yes/yes	49	1	-0.175	-2.508	yes/yes	147	6	-0.039	-1.965
$i^{l*}$	yes/yes	60	5	-0.050	-1.574	yes/yes	185	13	-0.016	-1.554
$i^l - i^{l*}$	yes/no	47	3	-0.375	-3.475**	yes/no	143	10	-0.120	-3.173**
$g$	yes/yes	98	7	-0.067	-2.176	yes/yes	293	24	-0.065	-2.210
$D$	yes/no	93	8	-0.097	-3.208**	yes/no	297	20	-0.032	-3.142***
$p^*$	yes/yes	62	4	-0.087	-1.149	yes/yes	196	5	-0.010	-2.342
$m$	yes/yes	92	13	-0.127	-1.827	yes/yes	294	23	-0.110	-2.539

Note:  $g$ ,  $D$ ,  $p^*$  and  $m$  have been subjected to seasonal adjustment as described in Appendix B.  $T$  is the number of observations included in the test. \*(\*\*)[\*\*\*] indicates that  $H_0: Z \sim I(k)$  where  $k > 0$  is rejected at the 10(5)[1] percent significance level. McKinnon (1991) critical values are used.

dication that the time series are non-stationary. Banerjee et al. (1993) discuss the properties of the regression estimates obtained when some of the variables are integrated, and find that what is often called balance in the regression is an important property. This means that when the dependent variable is stationary, the explanatory variables should also be integrated of order zero or cointegrated. Consequently, there is a need to test the integration order of the variables involved in the regressions.

To test the integration order of the individual series, I have used the augmented Dickey-Fuller (ADF) procedure and applied the practical guidelines proposed by Hamilton (1994), which means that a constant and/or linear trend is included in the regression if the variable displays a non-zero mean and/or sign of linear trend in the observed sample (see Figures 3 and 4). For which variables a constant and/or trend is included in the regressions are reported in Tables 3 and 4 below. In the ADF procedure,  $H_0$  is the hypothesis that the series under consideration is non-stationary, which in practice implies an estimated  $\hat{\phi}$  in Tables 3 and 4 not significantly lower than zero. The ADF test results for the variables in level form are reported in Table 3.

As seen from Table 3, the null hypothesis that the variables are non-stationary can only be re-

jected for  $i^s - i^{s*}$ ,  $i^l - i^{l*}$  and  $D$  on reasonable significance levels. Although we can reject the hypothesis that  $D$  is non-stationary, the estimated autoregressive coefficients are close to one, implying that our empirical estimate of  $\rho^D$  is also close to one. This finding is consistent with what we expected a priori, and discussed in Section 2.2. Thus, according to the theoretical model (11), the effects of government budget deficits on the nominal interest rate differentials are likely to be relatively small.

In order to determine the integration order for the other variables, we proceed to the  $I(1)$  tests. With quarterly and monthly frequencies, both first differences on seasonally adjusted data or annual changes on seasonal unadjusted data can be utilized in the tests. One of the aims of using annual changes is to eliminate most of the seasonal variability prior to estimation. In addition, the series obtained are often easier to interpret than first difference series, where the seasonal variability often completely swamps the remaining variability.<sup>20</sup> Thus, for  $i^{s*}$  and  $i^{l*}$ , the tests are based on first differences, and for  $g$ ,  $p^*$  and  $m$  on annual changes of seasonally unadjusted data.

<sup>20</sup> Furthermore, note that  $1-L^4 = (1-L)(1+L+L^2+L^3)$ , which shows that an analysis based on annual changes can be regarded as an analysis based on first differences on seasonally adjusted data.

Table 4. Augmented Dickey-Fuller tests of integration order on differences.

Variable	Quarterly frequency					Monthly frequency				
	const/ trend	$T$	$p$	$\hat{\phi}$	$t$ -value	const/ trend	$T$	$p$	$\hat{\phi}$	$t$ -value
$\Delta i^{s*}$	yes/no	58	0	-0.60	-4.938***	yes/no	166	12	-0.55	-3.649***
$\Delta i^{l*}$	yes/no	60	4	-1.19	-6.138***	yes/no	184	13	-0.81	-4.770***
$\Delta g$	yes/no	100	1	-0.26	-3.099***	yes/no	283	22	-0.24	-1.952**
$\Delta p^*$	yes/no	59	4	-0.07	-2.964**	yes/no	177	12	-0.03	-3.360***
$\Delta m$	yes/no	90	11	-0.43	-3.445**	yes/no	283	22	-0.41	-3.865***

Note: The tests are performed on first differences for  $i^{s*}$  and  $i^{l*}$ , and on annual changes on seasonally unadjusted data for  $g$ ,  $p^*$  and  $m$ .  $T$  is the number of observations included in the test.  $**$  ( $***$ ) indicates that  $H_0: Z \sim I(k)$  where  $k > 1$  is rejected at the 10 (5) [1] percent significance level. McKinnon (1991) critical values are used.

The overall impression from Table 4 is that the null hypothesis is firmly rejected, and together with the test results in Table 3, it is concluded that  $i^{s*}$ ,  $i^{l*}$ ,  $g$ ,  $p^*$  and  $m$  are non-stationary and integrated of order one.

The ADF tests above have shown that the dependent variables involved in the regression (11) are stationary, but that every explanatory variable except  $D$  is non-stationary. Consequently, we have the undesirable unbalanced regression case, where some variables involved are stationary and some non-stationary. Therefore, all the non-stationary variables in (11) are rewritten in difference form ( $i^{s*}$  and  $i^{l*}$  in first differences; annual changes for  $g$ ,  $p^*$  and  $m$ ), whereas the stationary variables ( $i^s - i^{s*}$ ,  $i^l - i^{l*}$  and  $D$ ) are in levels in the regression analysis to get balanced regressions.<sup>21</sup>

<sup>21</sup> An alternative approach would be to estimate a vector error correction model (VECM) for the whole system [ $p^*$   $i^{s*}$   $i^{l*}$   $g$   $D$   $m$   $i^s$   $i^l$ ] with the Johansen method; see Johansen (1988) and Johansen and Juselius (1990). In this study, however, I have chosen to use the restrictions from the conventional model directly to enable comparability with previous studies (e.g. Correia-Nunes and Stemitsiotis, 1995 and Evans, 1985, 1987a and 1987b). Moreover, as was noted in Section 2.3, if the variables  $p^*$ ,  $i^{s*}$ ,  $i^{l*}$ ,  $g$  and  $m$  follow unit root processes (i.e., the null that  $\rho^{p^*}(L)$ ,  $\rho^{i^{s*}}(L)$ ,  $\rho^{i^{l*}}(L)$ ,  $\rho^g(L)$  and  $\rho^m(L)$  equal 1 cannot be rejected), the conventional model suggested that these variables should not have any long-run influence on  $i^s - i^{s*}$  and  $i^l - i^{l*}$ . This suggests that the information loss of not using a VECM may not be severe. Finally, we have only about 50 quarterly observations, which is not too much data when estimating a VECM (see Gredenhoff and Jacobson, 2001).

#### 4.2 Econometric Issues

The estimated regression equations for the short- and long-term interest rate differentials include a lag polynomial in the stationary variable  $D$ , and lag polynomials in the stationary differences for the  $I(1)$  variables. Since the coefficient sums on the regressors in (11) have appropriate probability limits only if enough lagged values are included in the regressions, one should not be too parsimonious. On the other hand, the more extraneous regressors included, the less power when testing hypotheses. These two competing considerations have been balanced by including lagged values up to 3 years. The insignificant lagged values of each variable were then removed so that the most important dynamics were captured in the final estimated equations.<sup>22</sup> To give an indication of the estimated model's goodness of fit, the adjusted sample coefficients of determination,  $\bar{R}^2$ , are provided.

Before turning to the estimation results presented in Tables 6 and 7, a comment on the method used in the estimations is in order. First, estimation with OLS is based on the assumption that the error term is uncorrelated with the regressors. However, it is easy to argue that aggregate money, demand and supply shocks,

<sup>22</sup> In the estimations, I use Almon lags with no end point restrictions and allow for a third degree polynomial. The lag in effect may, by this procedure, be distributed as a straight line, a parabola or an "s-curve".

Table 5. Quarterly 2SLS with correction for serial correlation regressions.

	$i^s - i^{s*}$		$i^l - i^{l*}$	
	Coefficient sum	Lag length	Coefficient sum	Lag length
$\Delta g$	- 0.270*** (-2.59)	0	- 0.103** (-1.76)	0
$\Delta p^*$	1.973*** (4.53)	0	0.908*** (5.44)	10
$\Delta m$	- 0.076 (-0.76)	12	0.048** (1.63)	0
$\Delta i^{s*}$	- 1.594 (-1.15)	12	2.456*** (3.20)	9
$\Delta i^{l*}$	- 0.515*** (-1.95)	0	- 10.945*** (-6.12)	10
$D$	0.200** (3.07)	8	0.249*** (7.09)	8
$c$	- 5.813*** (-3.39)		- 2.253** (-3.27)	
<i>Dummy</i>	2.679*** (4.58)			
$p, q$	1,4		0,0	
$\bar{R}^2$	0.77		0.88	

Note: Simulated critical limits.  $c$  denotes the constant term and *Dummy* is a dummy variable equal to 1 1992:3 - 1992:4 and 0 otherwise. \* (\*\*) [\*\*\*] indicates that the coefficient is statistically significant at the 10 (5) [1] percent level according to the simulated distribution. Asymptotic  $t$ -statistics within parentheses. The samples consist of 44 and 47 observations, respectively. Lagged dependent and explanatory variables have been used as instruments.  $p$  and  $q$  denote the order of the ARMA( $p, q$ ) process for the residual in the estimations.

contained in the residual  $v_t^r$ , also have contemporaneous effects on the regressors  $g$ ,  $D$  and  $m$ . As a consequence of this, the OLS estimates of the coefficient sums in (11) are very likely to be inconsistent. The inconsistencies can be serious and of either sign, depending on how important each source of endogeneity is. In this paper, I have tried to overcome this problem by estimating the models with the Two-Stage Least Squares (2SLS) method with correction for serial correlation suggested by Fair (1970). Fair shows that consistent estimates can be obtained when the residuals are serially correlated, if lagged values of the regressors and the dependent variable are used as instruments and the estimated residual is explicitly modelled as an ARMA( $p, q$ ) process. The reason not to use 2SLS without serial correction is, as discussed in Section 2.3, that we expect the residuals to be serially correlated. Therefore, an augmented ARMA( $p, q$ )-process  $v_t^r = \rho_1^r v_{t-1}^r + \dots + \rho_p^r v_{t-p}^r + \varepsilon_t^r + \theta_1^r \varepsilon_{t-1}^r + \dots + \theta_q^r \varepsilon_{t-q}^r$  was included in the 2SLS estimations of (11), until the Ljung-Box

( $LB$ ) statistic indicated absence of serial correlation in the residuals.

Finally, since I have a limited number of observations in the regressions, I have simulated the critical values reported in Tables 6 and 7 below to get the correct small sample significance levels. In the simulations, I first estimated and then simulated (10) on quarterly and monthly data to get a sample of the same size as used in the regressions reported in Tables 5 and 6 for the independent variables, which were then used to generate  $i^s - i^{s*}$  and  $i^l - i^{l*}$ . Finally, I used the simulated dependent and independent variables to estimate the regressions in the Tables 5 and 6. To get small sample distributions for the coefficient sums, I repeated this procedure until the simulated distributions converged in mean and variance.<sup>23</sup> To get a feeling for the

<sup>23</sup> In practice, it took approximately 1000 repetitions on both the monthly and quarterly frequency for the simulated distributions to converge according to the mean-variance criteria.

importance of the small sample significance levels, the asymptotic  $t$ -statistics are also provided in parentheses.

### 4.3 Results

Table 5 reports that the coefficient sums for  $D$  are indeed positive and strongly statistically significant on the quarterly frequency. The estimated coefficient sums are 0.20 and 0.25, suggesting that a one percentage unit increase in the government budget deficit as a ratio of GDP leads to an increase in the short- and long-term nominal interest rate differentials by 0.20 and 0.25 percentage points respectively after two years' time. These figures are close to point estimates reported by Correia-Nunes and Stemitiotis (1995) for Japan (0.21), Germany (0.22) and Ireland (0.22), but are lower than their estimate for the United States (0.79) using yearly data.

Among the other regressors, the short-run dynamics for  $g$  and  $p^*$  are most important, although their estimated parameters have opposite signs. A dummy variable has also been included in the regression for the short-term interest rate differential to capture the effects of the interventions of Sveriges Riksbank (Bank of Sweden) on the market for short-term bills in September to November 1992. This "intervention effect" is easily seen in Figure 3. Implicitly, this dummy variable is likely to capture the extreme events within the target zone exchange rate regime that prevailed in Sweden until November 1992.<sup>24</sup>

On the monthly frequency, as seen from Table 6, the estimated coefficient sums for  $D$  are still positive and highly significant, although they are lower than in the quarterly regressions. This can be taken as an indication of that lower (quarterly or yearly) data frequencies are more supportive for the conventional view than higher (monthly), as noted in the introduction. But

here, due to the large sample variability for the budget deficit, we were able to identify positive effects of the budget deficit on interest rates also on monthly data.

Comparison of the Tables 5 and 6 also reveals that the lag length effect of  $D$  is the same in both the quarterly and monthly regressions. For the other variables, the most pronounced difference is that the estimated coefficient for  $g$  is positive, in contrast to the quarterly regressions. This may be an indication that our interpolation measure of  $G$  is flawed on the monthly frequency. Unlike the quarterly regressions, the estimated coefficient sums for  $m$  are now negative/positive and statistically significant/insignificant for  $i^s - i^{s*}/i^l - i^{l*}$ . We also see that  $i^{s*}$  and  $i^{l*}$  now become highly significant in the regression for  $i^s - i^{s*}$ , while the short-run dynamics for  $p^*$  still are positive but not statistically significant. Finally, the estimated parameter for the dummy variable is higher, since the variable can be defined in a more appropriate way with monthly data.

Finally, a general comment on the estimation results is warranted. We noticed that the model in (11) did not suggest sign uniqueness of the coefficient sums estimated above. Consequently, one cannot reject the conventional macro model either on the basis that the estimated coefficient sums for the variables were not statistically significant or because they have the "wrong" sign. Given this and that the models goodness-of-fit criterion ( $\bar{R}^2$ ) was found to be satisfactory, the evidence presented in this paper is consistent with the predictions of the conventional model.

In accordance with many other countries, Sweden went from a fixed to a managed floating exchange rate regime in November 1992, and in January 1993, the Swedish central bank announced the new inflation targeting/floating exchange rate regime. In this paper, I have used data from both the fixed and floating regimes to get sufficiently many observations in the regressions. Therefore, it is desirable to test whether the structure of the regressions reported in Tables 5 and 6 is the same after the regime shift. The standard test available for this purpose is the Chow test, in which the basic idea is to compare the results of separate esti-

<sup>24</sup> Interestingly, parameter stability in the model of the short-term interest rate differential is only preserved if this dummy is included (see Table 7), which suggests that the exchange rate regime was important during this extreme period but that the same model can be applied to all other periods during the two exchange rate regimes that are spanned by the sample.



Table 6. Monthly 2SLS with correction for serial correlation regressions.

	$i^s - i^{s*}$		$i^l - i^{l*}$	
	Coefficient sum	Lag length	Coefficient sum	Lag length
$\Delta g$	0.114*** (3.20)	0	0.007* (0.80)	0
$\Delta p^*$	0.160 (0.85)	11	0.090 (0.57)	24
$\Delta m$	- 0.195 *** (-4.18)	4	- 0.064 (-1.25)	12
$\Delta i^{s*}$	8.410*** (3.84)	24	5.491*** (3.17)	24
$\Delta i^{l*}$	- 10.127*** (-3.23)	16	- 12.611*** (-3.55)	24
$D$	0.142*** (3.39)	24	0.113*** (3.13)	24
$c$	1.347 (1.74)		1.280 (1.97)	
<i>Dummy</i>	3.667*** (7.27)			
$p, q$	0,1		0,3	
$\bar{R}^2$	0.76		0.88	

Note: Simulated critical limits.  $c$  denotes the constant term and *Dummy* is a dummy variable equal to 1 1992:09 and 1992:11, 0 otherwise. \*(\*\*)[\*\*\*] indicates that the coefficient is statistically significant at the 10 (5) [1] percent level according to the simulated distribution. Asymptotic  $t$ -statistics within parentheses. The samples consist of 148 in both regressions. Lagged dependent and explanatory variables have been used as instruments.  $p$  and  $q$  denote the order of the ARMA( $p, q$ ) process for the residual in the estimations.

Table 7. Chow test for structural stability.

Test statistic	Quarterly regressions		Monthly regressions	
	$i^s - i^{s*}$	$i^l - i^{l*}$	$i^s - i^{s*}$	$i^l - i^{l*}$
$F^{obs}$	1.511	1.380	0.892	1.196
$p$ -value	0.241	0.273	0.652	0.244

Note:  $n_{fi}$  is equal to 13 (1993Q2 – 1996Q2) on quarterly data and 41 (1993:2 – 1996:6) on monthly data, while  $n_{fi}$  is equal to 31 (1985Q3 – 1993Q1) and 34 (1984Q4 – 1993Q1) on quarterly data and 107 (1984:03 – 1993:1) on monthly data for  $i^s - i^{s*}$  and  $i^l - i^{l*}$  respectively.

mations in the two subperiods (fixed and floating regime periods) and the complete period under the null hypothesis that the structure of the model is unchanged.<sup>25</sup> In Table 7, we report the test results.

As seen from Table 7, we never reject the null hypothesis of an unchanged structure at standard significance levels. It therefore seems as if the results reported in Tables 5 and 6 are

<sup>25</sup> Since the original Chow-test is impossible to use in our case due to the short floating exchange rate regime period, I have used a modification of the test, sometimes called the Chow forecast test. If the model structure is un-

changed, the statistic  $F^{obs} = \frac{\hat{\sigma}_T^2 + (\hat{\sigma}_T^2 - \hat{\sigma}_R^2) \frac{(n_{fi} - k)}{n_{fi}}}{\hat{\sigma}_R^2}$  follows the  $F$ -distribution with  $n_{fi}$  and  $n_{fi} - k$  degrees of freedom, where

$n_{fi}$  = number of observations in the fixed exchange rate regime period,  $n_{fi}$  = number of observations in the managed floating exchange rate regime period,  $k$  = number of estimated parameters,  $\hat{\sigma}_T^2$  = estimated residual variance in the complete period and  $\hat{\sigma}_R^2$  = estimated residual variance in the fixed exchange rate regime period. If the residual variance is unchanged, the value of  $F^{obs}$  is 1. A change in structure should lead to a large residual variance for the complete period, with a consequent  $F^{obs}$  that is larger than 1.

robust with respect to the exchange rate/money regime shift in Sweden.

## 5. Concluding remarks

In this paper I have tried to shed some new light upon the empirical relation between nominal interest rates and government budget deficits. The strategy employed is similar to that of Evans (1985, 1987a, 1987b, 1988) in the sense that I have used a conventional macro model as my point of departure for the empirical investigation. But on the basis of a survey, I have also taken into account what seem to be the most important lessons from the previous empirical literature.

The cited literature suggests two factors that may account for the different empirical results in the previous literature. First of all, the treatment of the expected inflation rate seems to be of considerable importance; the results tend to be more supportive for the conventional view when a proxy is used to account for the expected inflation rate, rather than a reduced form. Second, the data frequency seems to be important. In studies which have exploited lower frequency data, the evidence is more in favor of the conventional than the Ricardian view. In order to control for the first factor, I have constructed and used a conventional model in which it is possible to solve for the rational inflation expectations analytically. To take the latter factor into proper account, I have used both quarterly and monthly data in the estimations.

The theoretical analysis shows that the conventional macro model developed here, in contrast to the findings in the previous literature, does not imply sign uniqueness for the sum of the elements in the parameter polynomials for the budget deficit in the regression equations for the short- and long-term nominal interest rates. However, in the special case when the budget deficit is assumed to follow an autoregressive process, the model implies that the coefficient sum of the elements in the parameter polynomials for the budget deficit should be positive, although individual elements may be negative, given that the budget deficit is a stationary process. Thus, the model offers three important

insights for empirical investigations of this issue. First, it stresses the importance of a careful determination of the number of lags for the regressors; if an insufficient number of lags for the government budget deficit are included in the regressions, the estimated coefficient sums may be close to zero. Second, if the persistence in the budget deficit is sufficiently high, the estimated coefficient sums for the budget deficit will be close to zero regardless of how many lags one includes in the estimations; however, it should be emphasized that this is a (small) open economy result. Consequently, the lack of a robust finding between budget deficits and interest rates should not necessarily be interpreted as evidence against the conventional view and indirect support for the Ricardian equivalence theorem, as claimed, for instance, by Evans (1987a) and Plosser (1987). Third, it is very hard to pin down the true effect of budget deficits on interest rates since the tests will have low power if the null hypothesis is close to the alternative. This stresses the need to use data with high sample variability in empirical work on this issue.

The empirical study utilizes data for Sweden, a small open economy that has suffered from very large swings in government budget deficits and interest rates compared to previous studies. In this sense, the empirical results here ought to be more reliable than those of previous studies. The results presented in the paper provide evidence for the conventional view in macroeconomics that larger government budget deficits produce higher nominal interest rates.

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